

# Math Skills

## Power

After you study each sample problem and solution, work out the practice problems on a separate sheet of paper. Write your answers in the spaces provided.

### PROBLEM

The world's most powerful tugboats, which are built in Finland, are capable of providing  $8.17 \times 10^6$  W of power. How much work does one of these tugboats do in 12.0 s?

### SOLUTION

**Step 1: List the given and unknown values.**

**Given:** *power*,  $P = 8.17 \times 10^6$  W  
*time*,  $t = 12.0$  s

**Unknown:** *work*,  $W = ?$  J

**Step 2: Rearrange the power equation to solve for work.**

$$\text{power} = \frac{\text{work}}{\text{time}} \qquad P = \frac{W}{t}$$

$$P \times t = \frac{W}{t} \times t = W$$

**Step 3: Insert the known values into the equation, and solve.**

$$W = (8.17 \times 10^6 \text{ W}) \times (12.0 \text{ s}) = (8.17 \times 10^6 \text{ J/s}) \times (12.0 \text{ s})$$

$$W = 9.80 \times 10^7 \text{ J}$$

### PRACTICE

- One horsepower (1 hp) is the unit of power based on the work that a horse can do in one second. This is defined, in English units, as a force of 550 lb that can move an object 1 ft in 1 s. In SI, 1 hp equals 745.7 W. Suppose you have a horse that has a power output of 750 W. How much work does this horse do in 0.55 s?  

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- A race car with a 255 hp ( $1.90 \times 10^5$  W) engine is able to accelerate from rest to its top speed in 9.00 s. How much work does the car's engine do in this interval of time?  

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- A ship's diesel engine has a power output of 13.0 W ( $13.0 \times 10^6$  W). How much work is done by this engine in 15.0 min?

Math Skills *continued***PROBLEM**

Suppose a weightlifter's power output is 178 W during the time he does 3,310 J of work on the weights. How long does it take the weightlifter to raise the weights?

**SOLUTION**

**Step 1:** List the given and unknown values.

**Given:** power,  $P = 178 \text{ W}$

work,  $W = 3,310 \text{ J}$

**Unknown:** time,  $t = ? \text{ s}$

**Step 2:** Rearrange the power equation to solve for time.

$$\text{power} = \frac{\text{work}}{\text{time}} \qquad P = \frac{W}{t}$$

$$P \times \frac{t}{P} = \frac{W}{t} \times \frac{t}{P} = \frac{W}{P}$$

**Step 3:** Insert the known values into the equation, and solve.

$$t = \frac{3310 \text{ J}}{178 \text{ W}} = \frac{3310 \text{ J}}{178 \text{ J/s}}$$

$$t = 18.6 \text{ s}$$

**PRACTICE**

4. In order to sail through the frozen Arctic Ocean, the most powerful icebreaker ever built was constructed in the former Soviet Union. At the heart of the ship's power plant is a nuclear reactor with a power output of  $5.60 \times 10^7 \text{ W}$ . How long will it take for this power plant to do  $5.35 \times 10^{10} \text{ J}$  of work?

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5. The heaviest loads ever raised were part of the offshore Ekofisk complex in the North Sea. The  $4.0 \times 10^7 \text{ kg}$  complex was raised 6.5 m by over a hundred hydraulic jacks. The work done on the complex during the raising was approximately  $2.6 \times 10^{11} \text{ J}$ . Suppose the power output of all the jacks was  $5.7 \times 10^8 \text{ W}$ . How long did it take the jacks to raise the complex?

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6. Borax was mined in Death Valley, California, during the nineteenth century. It was transported from the valley by massive wagons, each pulled by a team of 21 mules. Suppose each mule's power output was 746 W (about 1 hp). If in a certain time interval the total work done by the team on the wagon was  $2.35 \times 10^7 \text{ J}$ , how long was that interval of time?

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Math Skills *continued*

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**PROBLEM**

A certain crane is able to lift  $2.20 \times 10^6$  kg. If the crane is able to raise this mass a distance of 20.0 m by doing  $4.32 \times 10^8$  J of work in 35.0 s, how much power has the crane provided?

**SOLUTION**

**Step 1: List the given and unknown values.**

**Given:** work,  $W = 4.32 \times 10^8$  J

time,  $t = 35.0$  s

The distance of 20.0 m and the mass of  $2.20 \times 10^6$  kg are not needed to calculate power.

**Unknown:** power,  $P = ?$  W

**Step 2: Write out the equation for power.**

$$\text{power} = \frac{\text{work}}{\text{time}} \qquad P = \frac{W}{t}$$

**Step 3: Insert the known values into the equation, and solve.**

$$P = \frac{4.32 \times 10^8 \text{ J}}{35 \text{ s}} = 1.2 \times 10^7 \text{ J/s} = 1.2 \times 10^7 \text{ W}$$

$$P = 12 \text{ MW}$$

**PRACTICE**

7. A certain steam turbine is designed to be used as both a power generator and as a pump. When used as a generator, the turbine provides enough power to do  $3 \times 10^{10}$  J of work in 1 min. What is the power output of the turbine?
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8. The space shuttle, which was first launched on April 12, 1981, is the world's first reusable space vehicle. The shuttle is placed in orbit by three engines that do  $1.4 \times 10^{13}$  J of work in 8.5 min. What is the power output of these engines?
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9. Lithuania's major nuclear power plant has one of the world's most powerful generators, which has a power output of  $1.45 \times 10^9$  W. How long must this generator run if it is to provide the energy to do  $4.35 \times 10^{11}$  J of work?
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